

①

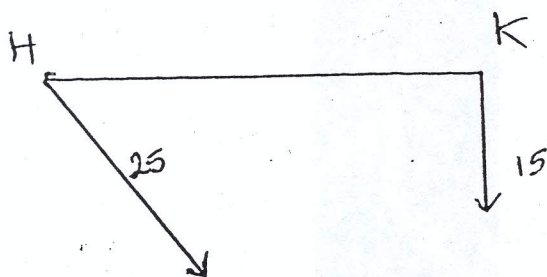
1987

Relative Velocity ①

Oliver
Murphy ©

At a certain instant a ship H is 37.5 km due West of a ship K. Ship H is travelling SE at 25 km/h and ship K is travelling South at 15 km/h.

- (i) Draw a diagram to show the velocity of K relative to H and calculate its magnitude and direction.
- (ii) If H and K can exchange signals when they are not more than 20 km apart, calculate when they can begin to exchange signals and for how long they can continue to exchange signals.

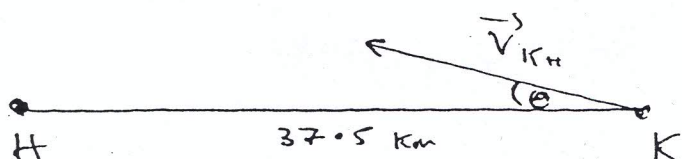


$$\begin{aligned}\vec{V}_H &= 25 \cos 45^\circ \vec{i} - 25 \sin 45^\circ \vec{j} \\ &= 25(-0.7071) \vec{i} - 25(-0.7071) \vec{j} \\ &= 17.68 \vec{i} - 17.68 \vec{j}\end{aligned}$$

$$\vec{V}_K = -15 \vec{j}$$

$$\begin{aligned}\therefore \vec{V}_{KH} &= \vec{V}_K - \vec{V}_H = -15 \vec{j} - (17.68 \vec{i} - 17.68 \vec{j}) \\ &= -17.68 \vec{i} + 2.68 \vec{j}\end{aligned}$$

(Back a lot
up a little)



$$|\vec{V}_{KH}| = \sqrt{(-17.68)^2 + (2.68)^2} = \sqrt{319.68} = 17.88 \text{ km/h}$$

$$\tan \theta = \frac{2.68}{17.68} = 0.1516 \Rightarrow \theta = \tan^{-1}(0.1516) = 8.61^\circ$$

Direction is W 8.61° N.